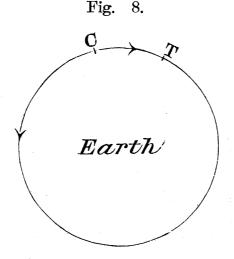
may be, as Professor H. Nagaoka suggests, one of the maximum transit velocity; or may mark the limit beyond which the seismic waves are, on account of certain physical properties of the underlying medium, unable to penetrate. Further, the consideration on the transit velocity of the Caracas earthquake of 1900 (§ 55) seems to indicate that, the waves with the transit velocity  $v_2$  also travel along a layer parallel to the surface of the earth.

That the waves with the transit velocity  $v_5$ , or those in the 3rd phase of the principal portion, travel along the surface of the earth is perfectly evident. (See also § 46.)

## XV. Propagation of Seismic Waves completely round the Earth.

§ 44. Let T (Fig. 9) be the observing station (Tōkyō), and C the earthquake origin. Then there are three sets of motion, which



we may call respectively  $W_1$ ,  $W_2$ , and  $W_3$  waves, as follows:—firstly, the  $W_1$  waves are those propagated from C to T along the shortest surface path; secondly, the  $W_2$  waves are those propagated from C in the opposite direction and reach T after passing through the antipode of C; and thirdly, the  $W_3$  waves are the  $W_1$  waves propagated further in the same direction, beyond T, and again reach

the latter after once completely travelling round the earth. (Fig. 9, which is the NS component diagram of the Turkestan earthquake of Aug. 22, 1902, recorded at Hongō, Tōkyō, indicated the  $W_2$  and  $W_3$  waves distinctly.)

The identification of the  $W_3$  waves is possible only in a very few number of cases; that of the  $W_2$  waves is, however, more definite, being usually characterized by the fact that their period is much slower than those of the preceding vibrations, which form the end portion of the  $W_1$  waves, or the earthquake proper.

Table XXXVII gives the time observations in Tōkyō relating to the three sets of waves,  $W_1$ ,  $W_2$ , and  $W_3$ , in cases of the twelve distant earthquakes, of which the first nine, (b), (c), (e), (f), (g), (h), (i), (j) and (k), are the same as those considered in the previous section, while the remaining three, (l), (m) and (n), have been newly added.

for allowed from formal formal formal formal formation of the formal for Commencement of Ind prel. tremor. Connecement of Egie. (Observed with Omori's Horizontal Pendulum at Hongo, Tokyo.) NS Component. Multiplication=10. (W3 waves) Commencement of 1<sup>st</sup> phase of princ. portion.

Fig. 9. Turkestan Earthquake of Aug. 22, 1902; 0.9.33. p.m.

Time: I tick interval=Iminute.

**TABLE XXXVII.**EARTHQUAKES PROPAGATED ROUND THE EARTH.\*

Eq.	Date.	Origin.	Commencement of the eqke.	3rd phase of the princ. portion.	Commence- ment of W <sub>2</sub> waves.	Commence- ment of W <sub>3</sub> waves.
b	Sept. 11,1899.	Alasea.	h m s 6, 50, 58 a.m.	h m s 7. 10. 01 a.m.	h m s 9.18.48 a.m.	h m s
c	,, 20, ,,	Aidin.	11. 24. 27 a.m.	11. 58. 46 a.m.	1.05.34 p.m.	
e	Jan. 20,1900.	Mexico.	3. 52. 39 p m.	4. 30. 13 p.m.	5. 20. 50 p.m.	<del></del>
$\mathbf{f}$	Sept. 18, ,,	_	7. 1.41 a.m.	7. 14. 31 a.m.	9. 48. 41 a.m.	
g	Oct. 9, "	Alasca.	9. 37. 14 p m.	9. 53. 45 a.m.	0.27.36 p.m.	_
h	,, 29, ,,	Caracas.	6. 29. 22 p.m.	7. 16. 55 p.m.	8.08.47 p.m.	_
i	April 19,1902.	Guatemala,	11. 38. 47 a.m.	0. 20. 24 p.m.	1.01.36 p.m.	
j	Aug. 22, "	Kashgar.	0. 9.33 p.m.	0.28.01 p.m.	2. 55. 18 p.m.	3. 50. 15 p.m.
k	Sept. 22, "	Guam.	10. 52. 16 a.m.	10. 58. 22 a.m.	1.52.39 p.m.	2.12.24 p.m.
1 .	June 22,1900.		6. 11. 09 a.m.	6. 54. 29 a.m.		9.47.49 p.m.
m	July 29, "		4. 08. 42 p.m.	4. 26. 33 p.m.		8. 20. 02 p.m.
n	Aug. 14, "		5. 19. 39 a.m.	5. 26. 25 a.m.	8.00.28 a.m.	

- § 45. Period and Range of motion of the  $W_1$ ,  $W_2$  and  $W_3$  waves. Table XXXVIII gives the period and the maximum range of motion of the three sets of waves, namely,  $W_1$ ,  $W_2$ , and  $W_3$  waves, in the twelve earthquakes contained in Table XXXVII; the part of the  $W_1$  waves taken for comparison being the 3rd phase of the principal portion.
- 1. Period. The average period of the  $W_2$  waves is with a few exceptions very uniform, and gives a mean value of 20,4 sec., which is identical with the predominating period in the 3rd phase of the principal portion (see also  $\S$  39); the period of the  $W_3$  waves being probably nearly the same as that of the  $W_2$  waves. These facts seem to indicate that the  $W_2$  and  $W_3$  waves are the same vibrations

<sup>\*</sup> The times are given in the 1st Normal Japan Time.

which constitute the 3rd phase of the principal portion of the earth-quake proper. That this is probably the case may easily be understood, as the vibrations in the 3rd phase of the principal portion have large amplitude, while their period is tolerably slow, but not so very long as that of the waves in the 1st and the 2nd phases of the same portion.

2. Amplitude. The amplitude of the  $W_2$  waves is generally very much smaller than that of the  $W_1$  waves; the motion of the  $W_3$  waves being again much smaller than that of the  $W_2$  waves. This ought of course to be the case, as the intensity of the seismic waves rapidly decreases with an increase of distance from the centre of disturbance.

TABLE XXXVIII. MAX. 2a AND AVERAGE PERIOD IN THE W  $_1,$   $W_2$  AND  $W_3$  WAVES.

Eqke.	3rd phase. of princ. portion.		$W_2$ waves.		W <sub>3</sub> waves.	
No.	Max. 2a.	Principal Aver. period.	Max. 2a.	Aver. period.	Max. 2a.	Aver. period.
<u></u>	mm 3,2	sec. 20,7	mm 0,05	sec. 24,7	mm	sec.
c	0,9	$\begin{array}{ c c c }\hline (24,3)\\18,3\end{array}$	0,03	15,9	<u> </u>	<u> </u>
e	0,25	21,0	0,13	20,3	—	
$\mathbf{f}$	2,20	22,4	0,04	19,2		
g	1,50	21,4	Small.	21,4	<u> </u>	
h	1,04	21,9	0,54	22,5	·	_
i	0,63	$\begin{array}{c c} 320,1\\ 34,3\end{array}$	0,31	28,4		
j	5,70	18,0	0,07	17,6	Small.	
k		_	Small.	19,5	Small.	19,5
1	0,38	19,3		_	0,05	19,2
m	4,3	22,9		_	Small.	13,9
n	0,49	8,8	Small.	14,9		
Mean *	1,87	<b>20,6</b> ; 8,8; 24,3; 34,3	mm 0,12	20,4	-	<b>19,4</b> ; 13,9

<sup>\*</sup> The period most frequently occurring are prin ed in fat characters.

- § 46. Velocity of propagation of the  $W_2$  and the  $W_3$  waves. Table XXXVIII contains the necessary data for the calculation of the transit velocity of the  $W_2$  and  $W_3$  waves; the significations of the different symbols being as follows:
  - x=shortest *surface* distance between Tōkyō and the origin of an earthquake;
  - $\triangle T'$  = time difference between the occurrence of the  $W_2$  waves and that of the 3rd phase of the principal portion;
  - $\triangle T''$ =time difference between the occurrence of the  $W_3$  waves and that of the 3rd phase of the principal portion.

TABLE XXXIX.

## CALCULATION OF THE TRANSIT VELOCITY OF THE $\mathrm{W_2}$ AND THE $\mathrm{W_3}$ WAVES.

State of the control of the second section of the second

Eqke.	Total duration of 1st and 2nd	km.	km km 40000—2x	W <sub>2</sub> waves.		W <sub>3</sub> waves.	
No.	prel. tremers	<b>30</b>		T' ·	Transit velocity.	△T″	Transit velocity.
b c	m s 14. 13 22. 19	6100 9200	27800 21600	h m s 2. 08. 47 1. 06. 48	$3.6 \frac{\text{km}}{\text{sec.}}$ $5.4$	h m s	<u>km</u>
e	21. 40	11000 (?)	18000 (?)	0. 50. 37	5,9 (?)	_	<del></del>
f g	9. 04 12. 27	4300* 5600*	314C0 288C0	2. 34. 10 2. 33. 50	3,4 3,1		
$\mathbf{h}$	32. 31	<b>142</b> 00	11600 (2)	0. 51. 52	3,7	· · · · · ·	· · · · · · · · · · · · · · · · · · ·
j	30. 20 13. 30	122C0 (?) 5700	15600 (?) 28600	0. 41. 12 2. 27. 17	6,3 (?) <b>3,2</b>	3. 22. 14	3,3
k 1	4. 04 33. 30	2200 13900*	35600 12200	2. 54. 17	3,4	3. 14. 02 2. 53. 20	3,4 3,8
m	12. 17	5600*	28800		. <del>-</del> 	3. 53. 29	2,9
n	4. 50	2600*	34800	2. 34. 03	3,8	·	<del>-</del>
Mean.		1	## ()		$3,7\frac{\mathrm{km}}{\mathrm{sec.}}$	h m s 3. 20. 46	$3.4 \frac{\mathrm{km}}{\mathrm{sec.}}$

<sup>\*</sup> The distances (x) marked with asterisks have been calculated by the formula x km = 6.54 y sec. + 720 km.

The transit velocity of the  $W_2$  waves is given by the equation:  $velocity = \frac{40000 km - 2x km}{\triangle T'}$ ; while the transit velocity of the  $W_3$  waves is given by the equation:  $velocity = \frac{40000 km}{\triangle T'}$ , the circumference of the earth being supposed roughly to be 40000 km. The mean values of the transit velocity is found to be  $3.7 \frac{km}{sec.}$  for the  $W_2$  waves and  $3.4 \frac{km}{sec.}$  for the  $W_3$  waves. These results, which are very gross approximations, are to be interpreted as indicating the transit velocity of  $3.3 \frac{km}{sec.}$ . In fact, the Turkestan earthquake (Eqke j), which showed clearly the commencement of the  $W_2$  and  $W_3$  waves, gave the velocities of 3.2 and  $3.3 \frac{km}{sec.}$  respectively for these two sets of waves.

The mean value of  $\triangle T''$ , which ought to be constant, is 3 h 20 m 46 s, being the time required by the seismic waves, whose velocity is  $v_5$ , to travel once completely round the earth.

## XVI. Longitudinal and Transverse Vibrations.

§ 47. In the strong motion area of great destructive earthquakes, the directions of the maximum motion at the different places converge, or are symmetrical, to the epifocal region. Again, it is well known that the macro-seismic motion at great distances from the origin consists mainly of horizontal vibrations. These facts seem to show that the most active part of the earthquake motion consists of the longitudinal waves; and we may suppose, therefore, that  $v_5$ , which is the transit velocity of the most active portion in the macro-seismic disturbances and also of the 3rd phase of the principal portion in distant earthquakes, characterizes the longitudinal component of the seismic motion. We have, however, no reason to suppose that